

Interval Estimation and Hypothesis Testing

Chapter 3

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Chapter 3:
Interval Estimation and Hypothesis Testing

- 3.1 Interval Estimation
- 3.2 Hypothesis Tests
- 3.3 Rejection Regions for Specific Alternatives
- 3.4 Examples of Hypothesis Tests
- 3.5 The *p*-value

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3.1 Interval Estimation

Assumptions of the Simple Linear Regression Model

•SR1. $y = \beta_1 + \beta_2 x + e$
•SR2. $E(e) = 0 \Leftrightarrow E(y) = \beta_1 + \beta_2 x$
•SR3. $\text{var}(e) = \sigma^2 = \text{var}(y)$
•SR4. $\text{cov}(e_i, e_j) = \text{cov}(y_i, y_j) = 0$
•SR5. The variable x is not random, and must take at least two different values.
•SR6. (optional) The values of e are normally distributed about their mean $e \sim N(0, \sigma^2)$

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3.1.1 The t-distribution

- The normal distribution of b_2 , the least squares estimator of β , is

$$b_2 \sim N\left(\beta_2, \frac{\sigma^2}{\sum(x_i - \bar{x})^2}\right)$$
- A standardized normal random variable is obtained from b_2 by subtracting its mean and dividing by its standard deviation:

$$Z = \frac{b_2 - \beta_2}{\sqrt{\sigma^2 / \sum(x_i - \bar{x})^2}} \sim N(0,1) \tag{3.1}$$
- The standardized random variable Z is normally distributed with mean 0 and variance 1.

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3.1.1 The t-distribution

$$P(-1.96 \leq Z \leq 1.96) = .95$$

$$P\left(-1.96 \leq \frac{b_2 - \beta_2}{\sqrt{\sigma^2 / \sum(x_i - \bar{x})^2}} \leq 1.96\right) = .95$$

$$P\left(b_2 - 1.96\sqrt{\sigma^2 / \sum(x_i - \bar{x})^2} \leq \beta_2 \leq b_2 + 1.96\sqrt{\sigma^2 / \sum(x_i - \bar{x})^2}\right) = .95$$

This defines an interval that has probability .95 of containing the parameter β_2 .

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3.1.1 The t-distribution

- The two endpoints $\left(b_2 \pm 1.96\sqrt{\sigma^2 / \sum(x_i - \bar{x})^2}\right)$ provide an interval estimator.
- In repeated sampling 95% of the intervals constructed this way will contain the true value of the parameter β_2 .
- This easy derivation of an interval estimator is based on the assumption SR6 and that we know the variance of the error term σ^2 .

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3.1.1 The t-distribution

- Replacing σ^2 with $\hat{\sigma}^2$ creates a random variable t :

$$t = \frac{b_2 - \beta_2}{\sqrt{\hat{\sigma}^2 / \sum (x_i - \bar{x})^2}} = \frac{b_2 - \beta_2}{\sqrt{\text{var}(b_2)}} = \frac{b_2 - \beta_2}{\text{se}(b_2)} \sim t_{(N-2)} \quad (3.2)$$

- The ratio $t = (b_2 - \beta_2) / \text{se}(b_2)$ has a t -distribution with $(N - 2)$ degrees of freedom, which we denote as $t \sim t_{(N-2)}$.

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3.1.1 The t-distribution

- In general we can say, if assumptions SR1-SR6 hold in the simple linear regression model, then

$$t = \frac{b_k - \beta_k}{\text{se}(b_k)} \sim t_{(N-2)} \text{ for } k = 1, 2 \quad (3.3)$$

- The t -distribution is a bell shaped curve centered at zero.
- It looks like the standard normal distribution, except it is more spread out, with a larger variance and thicker tails.
- The shape of the t -distribution is controlled by a single parameter called the **degrees of freedom**, often abbreviated as *df*.

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3.1.2 Obtaining Interval Estimates

- We can find a “critical value” from a t -distribution such that

$$P(t \geq t_c) = P(t \leq -t_c) = \alpha/2$$

where α is a probability often taken to be $\alpha = .01$ or $\alpha = .05$.

- The critical value t_c for degrees of freedom m is the percentile value $t_{(1-\alpha/2, m)}$.

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3.1.2 Obtaining Interval Estimates

Figure 3.1 Critical Values from a *t*-distribution

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3.1.2 Obtaining Interval Estimates

- Each shaded “tail” area contains $\alpha/2$ of the probability, so that $1-\alpha$ of the probability is contained in the center portion.
- Consequently, we can make the probability statement

$P(-t_c \leq t \leq t_c) = 1 - \alpha$
(3.4)

$$P\left[-t_c \leq \frac{b_k - \beta_k}{se(b_k)} \leq t_c\right] = 1 - \alpha$$

$P[b_k - t_c se(b_k) \leq \beta_k \leq b_k + t_c se(b_k)] = 1 - \alpha$
(3.5)

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3.1.3 An Illustration

- For the food expenditure data

$P[b_2 - 2.024se(b_2) \leq \beta_2 \leq b_2 + 2.024se(b_2)] = .95$
(3.6)

- The critical value $t_c = 2.024$, which is appropriate for $\alpha = .05$ and 38 degrees of freedom.
- To construct an interval estimate for β_2 we use the least squares estimate $b_2 = 10.21$ and its standard error

$$se(b_2) = \sqrt{\text{var}(b_2)} = \sqrt{4.38} = 2.09$$

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3.1.3 An Illustration

- A "95% confidence interval estimate" for β_2 :

$$b_2 \pm t_{.975} se(b_2) = 10.21 \pm 2.024(2.09) = [5.97, 14.45]$$

When the procedure we used is applied to many random samples of data from the same population, then 95% of all the interval estimates constructed using this procedure will contain the true parameter.

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3.1.4 The Repeated Sampling Context

Sample	b_1	$se(b_1)$	b_2	$se(b_2)$	$\hat{\sigma}^2$
1	131.69	40.58	6.48	1.96	7002.85
2	57.25	33.13	10.88	1.60	4668.63
3	103.91	37.22	8.14	1.79	5891.75
4	46.50	33.33	11.90	1.61	4722.58
5	84.23	41.15	9.29	1.98	7200.16
6	26.63	45.78	13.55	2.21	8911.43
7	64.21	32.03	10.93	1.54	4362.12
8	79.66	29.87	9.76	1.44	3793.83
9	97.30	29.14	8.05	1.41	3610.28
10	95.96	37.18	7.77	1.79	5878.71

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3.1.4 The Repeated Sampling Context

Sample	$b_1 - t_{.975} se(b_1)$	$b_1 + t_{.975} se(b_1)$	$b_2 - t_{.975} se(b_2)$	$b_2 + t_{.975} se(b_2)$
1	49.54	213.85	2.52	10.44
2	-9.83	124.32	7.65	14.12
3	28.56	179.26	4.51	11.77
4	-20.96	113.97	8.65	15.15
5	0.93	167.53	5.27	13.30
6	-66.04	119.30	9.08	18.02
7	-0.63	129.05	7.81	14.06
8	19.19	140.13	6.85	12.68
9	38.32	156.29	5.21	10.89
10	20.69	171.23	4.14	11.40

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3.2 Hypothesis Tests

Components of Hypothesis Tests

1. A null hypothesis, H_0
2. An alternative hypothesis, H_1
3. A test statistic
4. A rejection region
5. A conclusion

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3.2 Hypothesis Tests

- **The Null Hypothesis**
 The null hypothesis, which is denoted H_0 (*H-naught*), specifies a value for a regression parameter.
 The null hypothesis is stated $H_0 : \beta_k = c$, where c is a constant, and is an important value in the context of a specific regression model.

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3.2 Hypothesis Tests

- **The Alternative Hypothesis**
 Paired with every null hypothesis is a logical alternative hypothesis, H_1 , that we will accept if the null hypothesis is rejected.
 For the null hypothesis $H_0: \beta_k = c$ the three possible alternative hypotheses are:
 - $H_1 : \beta_k > c$
 - $H_1 : \beta_k < c$
 - $H_1 : \beta_k \neq c$

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3.2 Hypothesis Tests

- The Test Statistic

$$t = (b_k - \beta_k) / \text{se}(b_k) \sim t_{(N-2)}$$
- If the null hypothesis $H_0 : \beta_k = c$ is true, then we can substitute c for β_k and it follows that

$$t = \frac{b_k - c}{\text{se}(b_k)} \sim t_{(N-2)} \tag{3.7}$$

If the null hypothesis is *not true*, then the t -statistic in (3.7) does *not* have a t -distribution with $N - 2$ degrees of freedom.

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3.2 Hypothesis Tests

- The Rejection Region

The rejection region depends on the form of the alternative. It is the range of values of the test statistic that leads to *rejection* of the null hypothesis. It is possible to construct a rejection region only if we have:

 - a test statistic whose distribution is known when the null hypothesis is true
 - an alternative hypothesis
 - a level of significance

The level of significance α is usually chosen to be .01, .05 or .10.

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3.2 Hypothesis Tests

- A Conclusion

We make a correct decision if:

 - The null hypothesis is *false* and we decide to *reject* it.
 - The null hypothesis is *true* and we decide *not* to reject it.

Our decision is incorrect if:

 - The null hypothesis is *true* and we decide to *reject* it (a Type I error)
 - The null hypothesis is *false* and we decide *not* to reject it (a Type II error)

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3.3 Rejection Regions for Specific Alternatives

- 3.3.1. One-tail Tests with Alternative “Greater Than” ($>$)
- 3.3.2. One-tail Tests with Alternative “Less Than” ($<$)
- 3.3.3. Two-tail Tests with Alternative “Not Equal To” (\neq)

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3.3.1 One-tail Tests with Alternative “Greater Than” ($>$)

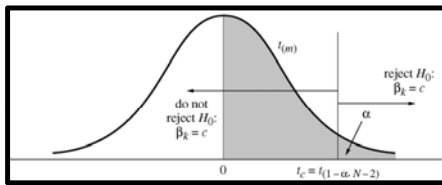


Figure 3.2 Rejection region for a one-tail test of $H_0: \beta_k = c$ against $H_1: \beta_k > c$

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3.3.1 One-tail Tests with Alternative “Greater Than” ($>$)

When testing the null hypothesis $H_0: \beta_k = c$ against the alternative hypothesis $H_1: \beta_k > c$, reject the null hypothesis and accept the alternative hypothesis if $t \geq t_{(1-\alpha, N-2)}$.

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3.3.2 One-tail Tests with Alternative "Less Than" (<)

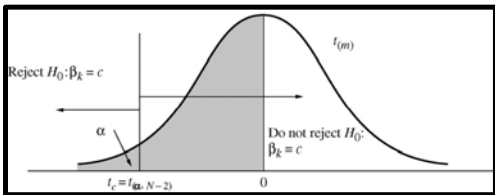


Figure 3.3 The rejection region for a one-tail test of $H_0: \beta_k = c$ against $H_1: \beta_k < c$

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3.3.2 One-tail Tests with Alternative "Less Than" (<)

When testing the null hypothesis $H_0: \beta_k = c$ against the alternative hypothesis $H_1: \beta_k < c$, reject the null hypothesis and accept the alternative hypothesis if $t \leq t_{(\alpha, N-2)}$.

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3.3.3 Two-tail Tests with Alternative "Not Equal To" (≠)

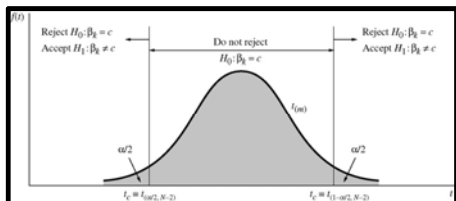


Figure 3.4 The rejection region for a two-tail test of $H_0: \beta_k = c$ against $H_1: \beta_k \neq c$

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3.3.3 Two-tail Tests with Alternative "Not Equal To" (\neq)

When testing the null hypothesis $H_0: \beta_k = c$ against the alternative hypothesis $H_1: \beta_k \neq c$, reject the null hypothesis and accept the alternative hypothesis if $t \leq t_{(1-\alpha/2, N-2)}$ or if $t \geq t_{(\alpha/2, N-2)}$.

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3.4 Examples of Hypothesis Tests

STEP-BY-STEP PROCEDURE FOR TESTING HYPOTHESES

1. Determine the null and alternative hypotheses.
2. Specify the test statistic and its distribution if the null hypothesis is true.
3. Select α and determine the rejection region.
4. Calculate the sample value of the test statistic.
5. State your conclusion.

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3.4.1 Right-tail Tests

3.4.1a One-tail Test of Significance

1. The null hypothesis is $H_0: \beta_2 = 0$.
The alternative hypothesis is $H_1: \beta_2 > 0$.
2. The test statistic is (3.7). In this case $c = 0$, so $t = b_2 / se(b_2) \sim t_{(N-2)}$ if the null hypothesis is true.
3. Let us select $\alpha = .05$. The critical value for the right-tail rejection region is the 95th percentile of the t -distribution with $N - 2 = 38$ degrees of freedom, $t_{(0.95, 38)} = 1.686$. Thus we will reject the null hypothesis if the calculated value of $t \geq 1.686$. If $t < 1.686$, we will not reject the null hypothesis.

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3.4.1 Right-tail Tests

- Using the food expenditure data, we found that $b_2 = 10.21$ with standard error $se(b_2) = 2.09$. The value of the test statistic is

$$t = \frac{b_2}{se(b_2)} = \frac{10.21}{2.09} = 4.88$$

- Since $t = 4.88 > 1.686$, we reject the null hypothesis that $\beta_2 = 0$ and accept the alternative that $\beta_2 > 0$. That is, we reject the hypothesis that there is no relationship between income and food expenditure, and conclude that there is a *statistically significant* positive relationship between household income and food expenditure.

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3.4.1 Right-tail Tests

3.4.1b One-tail Test of an Economic Hypothesis

- The null hypothesis is $H_0: \beta_2 \leq 5.5$.
The alternative hypothesis is $H_1: \beta_2 > 5.5$.
- The test statistic $t = (b_2 - 5.5)/se(b_2) \sim t_{(N-2)}$ if the null hypothesis is true.
- Let us select $\alpha = .01$. The critical value for the right-tail rejection region is the 99th percentile of the t -distribution with $N - 2 = 38$ degrees of freedom, $t_{(99,38)} = 2.429$. We will reject the null hypothesis if the calculated value of $t \geq 2.429$. If $t < 2.429$, we will not reject the null hypothesis.

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3.4.1 Right-tail Tests

- Using the food expenditure data, $b_2 = 10.21$ with standard error $se(b_2) = 2.09$. The value of the test statistic is

$$t = \frac{b_2 - 5.5}{se(b_2)} = \frac{10.21 - 5.5}{2.09} = 2.25$$

- Since $t = 2.25 < 2.429$ we do not reject the null hypothesis that $\beta_2 \leq 5.5$. We are *not* able to conclude that the new supermarket will be profitable and will not begin construction.

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3.4.2 Left-tail Tests

1. The null hypothesis is $H_0: \beta_2 \geq 15$.
The alternative hypothesis is $H_1: \beta_2 < 15$.
2. The test statistic $t = (b_2 - 15) / se(b_2) \sim t_{(N-2)}$
if the null hypothesis is true.
3. Let us select $\alpha = .05$. The critical value for the left-tail rejection region is the 5th percentile of the t -distribution with $N - 2 = 38$ degrees of freedom, $t_{(0.05, 38)} = -1.686$. We will reject the null hypothesis if the calculated value of $t \leq -1.686$. If $t > -1.686$, we will not reject the null hypothesis.

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3.4.2 Left-tail Tests

4. Using the food expenditure data, $b_2 = 10.21$ with standard error $se(b_2) = 2.09$. The value of the test statistic is
$$t = \frac{b_2 - 15}{se(b_2)} = \frac{10.21 - 15}{2.09} = -2.29$$
5. Since $t = -2.29 < -1.686$ we reject the null hypothesis that $\beta_2 \geq 15$ and accept the alternative that $\beta_2 < 15$. We conclude that households spend less than \$15 from each additional \$100 income on food.

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3.4.3 Two-tail Tests

3.4.3a Two-tail Test of an Economic Hypothesis

1. The null hypothesis is $H_0: \beta_2 = 7.5$.
The alternative hypothesis is $H_1: \beta_2 \neq 7.5$.
2. The test statistic $t = (b_2 - 7.5) / se(b_2) \sim t_{(N-2)}$
if the null hypothesis is true.
3. Let us select $\alpha = .05$. The critical values for this two-tail test are the 2.5-percentile $t_{(0.025, 38)} = -2.024$ and the 97.5-percentile $t_{(0.975, 38)} = 2.024$. Thus we will reject the null hypothesis if the calculated value of $t \geq 2.024$ or if $t \leq -2.024$. If $-2.024 < t < 2.024$, we will not reject the null hypothesis.

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3.4.3 Two-tail Tests

4. Using the food expenditure data, $b_2 = 10.21$ with standard error $se(b_2) = 2.09$. The value of the test statistic is

$$t = \frac{b_2 - 7.5}{se(b_2)} = \frac{10.21 - 7.5}{2.09} = 1.29$$

5. Since $-2.204 < t = 1.29 < 2.204$ we do not reject the null hypothesis that $\beta_2 = 7.5$. The sample data are consistent with the conjecture households will spend an additional \$7.50 per additional \$100 income on food.

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3.4.3 Two-tail Tests

3.4.3b Two-tail Test of Significance

- The null hypothesis is $H_0: \beta_2 = 0$.
The alternative hypothesis is $H_1: \beta_2 \neq 0$.
- The test statistic $t = b_2 / se(b_2) \sim t_{(n-2)}$
if the null hypothesis is true.
- Let us select $\alpha = .05$. The critical values for this two-tail test are the 2.5-percentile $t_{(.025, 38)} = -2.024$ and the 97.5-percentile $t_{(.975, 38)} = 2.024$. Thus we will reject the null hypothesis if the calculated value of $t \geq 2.024$ or if $t \leq -2.024$. If $-2.024 < t < 2.024$, we will not reject the null hypothesis.

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3.4.3 Two-tail Tests

4. Using the food expenditure data, $b_2 = 10.21$ with standard error $se(b_2) = 2.09$. The value of the test statistic is

$$t = \frac{b_2}{se(b_2)} = \frac{10.21}{2.09} = 4.88$$

5. Since $t = 4.88 > 2.204$ we reject the null hypothesis that $\beta_2 = 0$ and conclude that there is a statistically significant relationship between income and food expenditure.

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3.4.3 Two-tail Tests

Coefficient	Variable	Std. Error	t-Statistic	Prob.
83.41600	C	43.41016	1.921578	0.0622
10.20964	INCOME	2.093264	4.877381	0.0000

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3.5 The p-Value

p-value rule: Reject the null hypothesis when the p -value is less than, or equal to, the level of significance α . That is, if $p \leq \alpha$ then reject H_0 . If $p > \alpha$ then do not reject H_0 .

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3.5 The p-Value

If t is the calculated value of the t -statistic, then:

- if $H_1: \beta_k > c$, p = probability to the right of t
- if $H_1: \beta_k < c$, p = probability to the left of t
- if $H_1: \beta_k \neq c$, p = sum of probabilities to the right of $|t|$ and to the left of $-|t|$

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3.5.1 p -value for a Right-tail Test

Recall section 3.4.1b:

- The null hypothesis is $H_0: \beta_2 \leq 5.5$.
The alternative hypothesis is $H_1: \beta_2 > 5.5$.

$$t = \frac{b_2 - 5.5}{\text{se}(b_2)} = \frac{10.21 - 5.5}{2.09} = 2.25$$

- If $F_X(x)$ is the *cdf* for a random variable X , then for any value $x=c$ the cumulative probability is $P[X \leq c] = F_X(c)$.
- $p = P[t_{(38)} \geq 2.25] = 1 - P[t_{(38)} \leq 2.25] = 1 - .9848 = .0152$

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3.5.1 p -value for a Right-tail Test

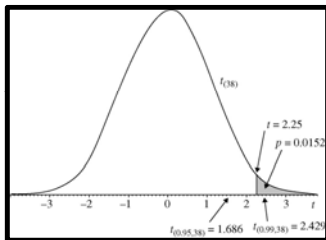


Figure 3.5 The p -value for a right tail test

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3.5.2 p -value for a Left-tail Test

Recall section 3.4.2:

- The null hypothesis is $H_0: \beta_2 \geq 15$.
The alternative hypothesis is $H_1: \beta_2 < 15$.

$$t = \frac{b_2 - 15}{\text{se}(b_2)} = \frac{10.21 - 15}{2.09} = -2.29$$

- $p = P[t_{(38)} \leq -2.29] = .0139$

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3.5.2 p -value for a Left-tail Test

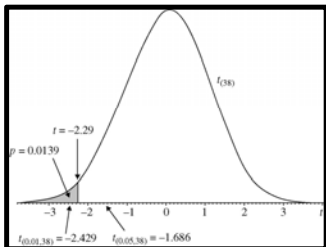


Figure 3.6 The p -value for a left tail test

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3.5.3 p -value for a Two-tail Test

Recall section 3.4.3a:

- The null hypothesis is $H_0: \beta_2 = 7.5$.

The alternative hypothesis is $H_1: \beta_2 \neq 7.5$.

$$t = \frac{b_2 - 7.5}{\text{se}(b_2)} = \frac{10.21 - 7.5}{2.09} = 1.29$$

- $p = P[t_{(38)} \geq 1.29] + P[t_{(38)} \leq -1.29] = .2033$

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3.5.3 p -value for a Two-tail Test

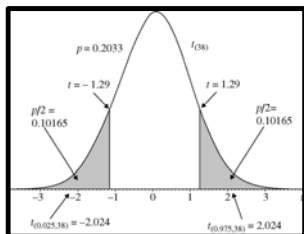


Figure 3.7 The p -value for a two-tail test

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Appendix 3A
Derivation of the t-distribution

$b_2 \sim N\left(\beta_2, \frac{\sigma^2}{\sum(x_i - \bar{x})^2}\right)$	
$Z = \frac{b_2 - \beta_2}{\sqrt{\text{var}(b_2)}} \sim N(0,1)$	(3A.1)
$\sum\left(\frac{e_i}{\sigma}\right)^2 = \left(\frac{e_1}{\sigma}\right)^2 + \left(\frac{e_2}{\sigma}\right)^2 + \dots + \left(\frac{e_N}{\sigma}\right)^2 \sim \chi^2_{(N)}$	(3A.2)
$V = \frac{\sum e_i^2}{\sigma^2} = \frac{(N-2)\hat{\sigma}^2}{\sigma^2}$	(3A.3)

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Appendix 3A
Derivation of the t-distribution

$V = \frac{(N-2)\hat{\sigma}^2}{\sigma^2} \sim \chi^2_{(N-2)}$	(3A.4)
$t = \frac{Z}{\sqrt{V/(N-2)}} = \frac{(b_2 - \beta_2) / \sqrt{\sigma^2 / \sum(x_i - \bar{x})^2}}{\sqrt{\frac{(N-2)\hat{\sigma}^2 / \sigma^2}{N-2}}}$ $= \frac{b_2 - \beta_2}{\sqrt{\frac{\hat{\sigma}^2}{\sum(x_i - \bar{x})^2}}} = \frac{b_2 - \beta_2}{\sqrt{\text{var}(b_2)}} = \frac{b_2 - \beta_2}{\text{se}(b_2)} \sim t_{(N-2)}$	(3A.5)

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Appendix 3B
Distribution of the t-statistic under H₁

$t = \frac{b_2 - 1}{\text{se}(b_2)} \sim t_{(N-2)}$	
$\frac{b_2 - c}{\sqrt{\text{var}(b_2)}} \sim N\left(\frac{1-c}{\sqrt{\text{var}(b_2)}}, 1\right)$	(3B.1)
where $\text{var}(b_2) = \frac{\sigma^2}{\sum(x_i - \bar{x})^2}$	

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